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Effect of off-axis ply orientation on UD fibre microbuckling

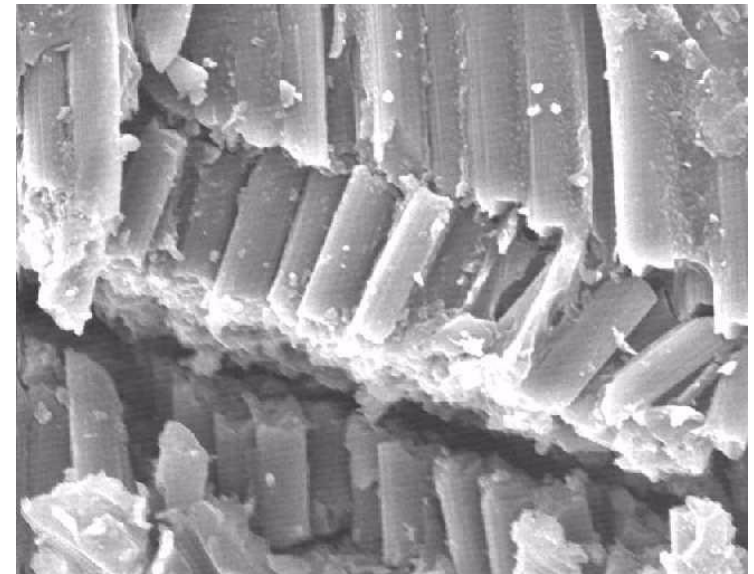
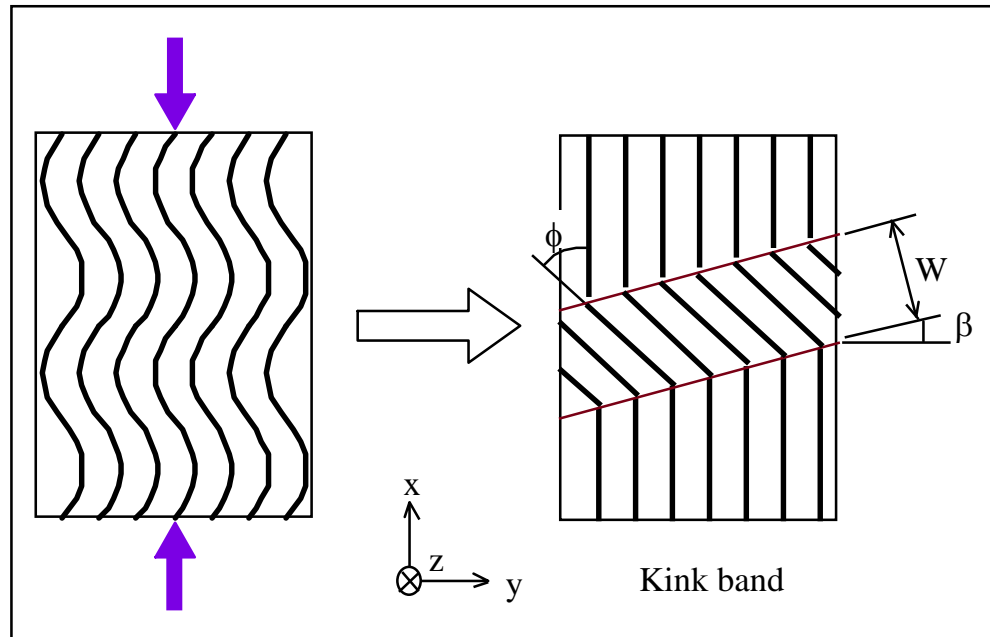
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Damage Mechanisms under Compression: Fibre microbuckling

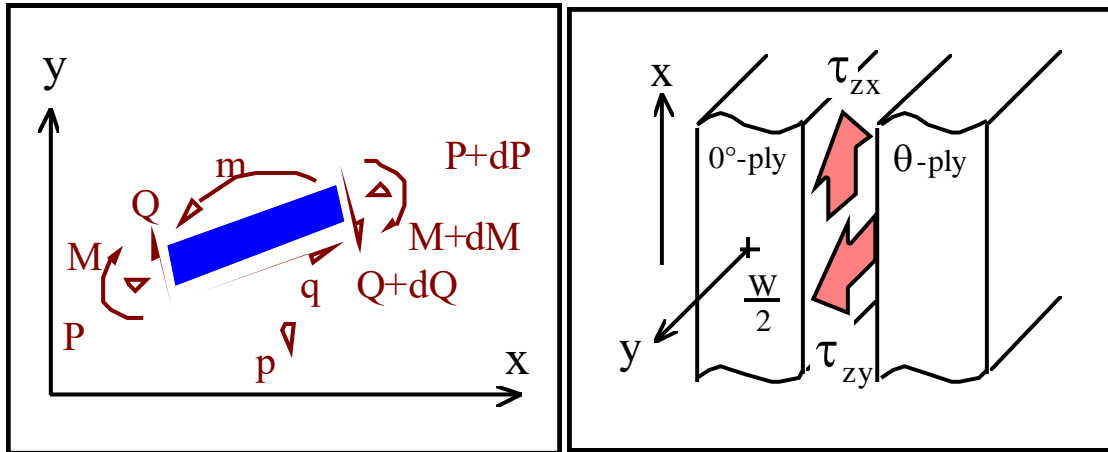
Compression failure of laminates occurs by fibre kinking of 0° -plies, immediately followed by delamination (catastrophic failure).



Kink band in multidirectional T800/924C laminate

0° fibre microbuckling initiation model

Berbinau, Soutis (1999)



$$v_0(x) = V_0 \cdot \sin\left(\frac{\pi x}{\lambda}\right)$$

$$p(s) = d_{\text{fibre}} (\tau_{zx} \vec{n} \cdot \vec{i} + \tau_{zy} \vec{n} \cdot \vec{j})$$

Equilibrium equation (fibre is modelled as a beam on a non-linear foundation)

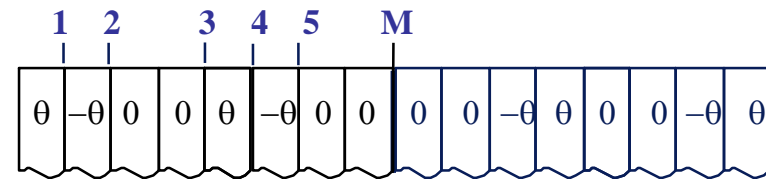
$$E_f I \frac{d^4(v - v_0)}{dx^4} + \frac{A_f \sigma_{0^\circ\text{-ply}}}{V_f} \cdot \frac{d^2 v}{dx^2} - 2 d_f \left\{ \left[\frac{d\tau_{zy}}{dy} \right]_{\frac{W}{2}} \right\} \cdot v - A_f G \left(\frac{d(v - v_0)}{dx} \right) \cdot \frac{d^2(v - v_0)}{dx^2} = 0$$

Non-linear differential equation that gives the compressive stress σ_0 of a 0° -ply in terms of the fibre maximum buckling amplitude V

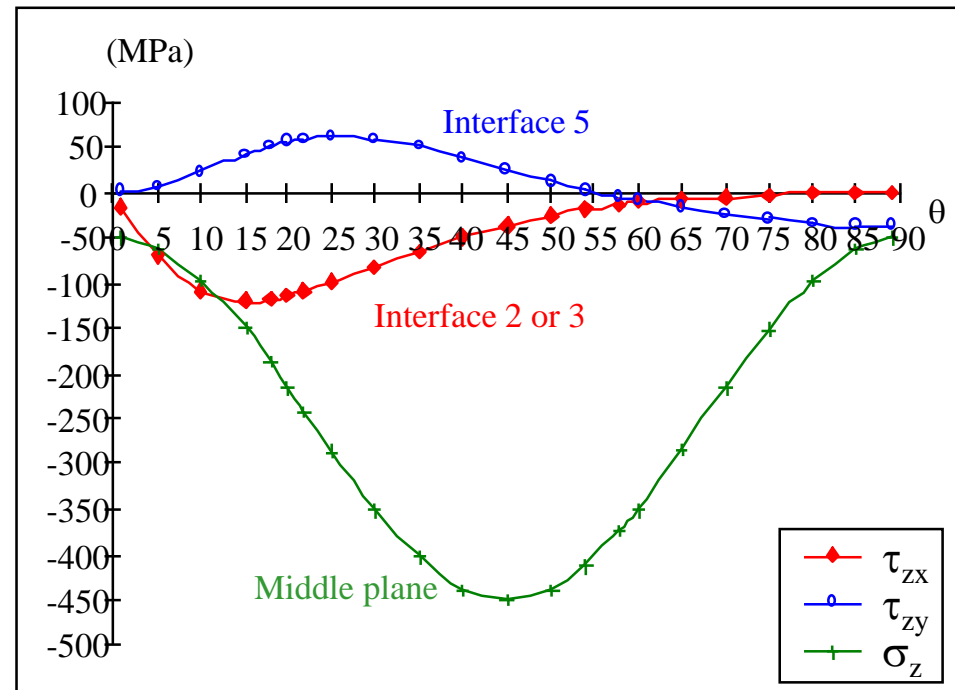
Free edge effect on fibre microbuckling

Berbinau, Soutis (1999)

- The microbuckling model of Berbinau, Soutis accounts for fibre properties, initial fibre waviness, ply interactions (interlaminar stresses), matrix non-linearity.



- Shear stress components are almost zero around 60°
- Normal component σ_z is compressive

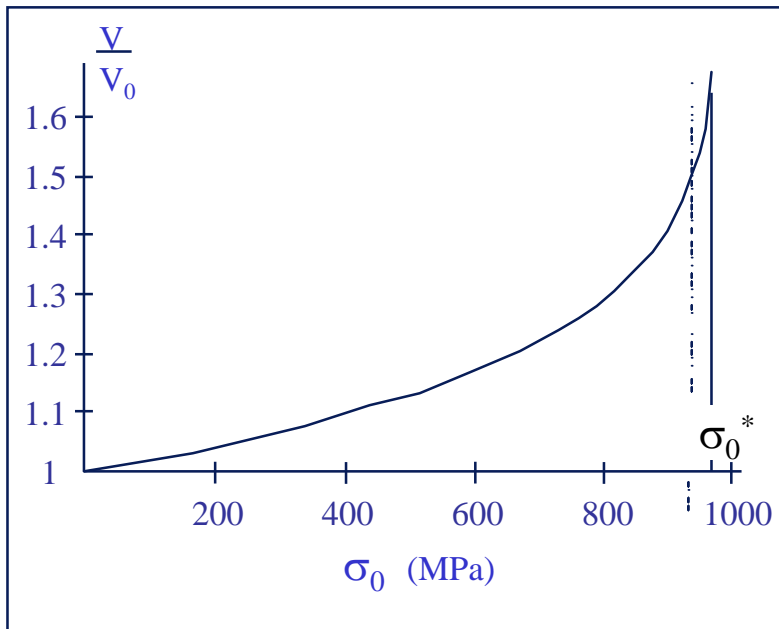


Maximum interlaminar edge stresses in a $[(\theta / -\theta / 0_2)_2]_s$ laminate (strain = 1%)

Fibre wavelength effect on fibre microbuckling triggering

Microbuckling amplitude:

$$\frac{V}{V_0} = f(\sigma_0)$$



Microbuckling amplitude V vs. stress on a 0° -ply σ_0 for $[(30/-30/0_2)_2]_s$

Off-axis ply orientation θ°	σ_0^* Fibre half-wavelength		
	$\lambda=10 \cdot d_{\text{fibre}}$	$\lambda=15 \cdot d_{\text{fibre}}$	$\lambda=20 \cdot d_{\text{fibre}}$
0	968	743	657
30	961	737	637
45	961	723	635
60	975	745	673
75	977	751	680
90	979	753	683

for $[(\theta/-\theta/0_2)_2]_s$ σ_0^* depends mostly on:

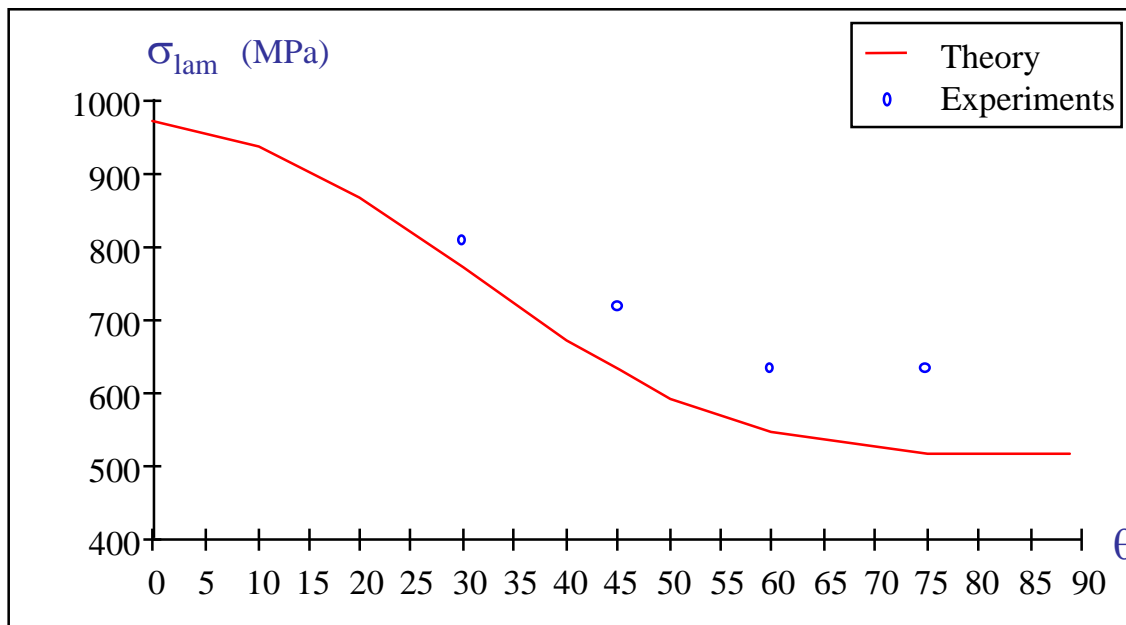
- fibre wavelength
- matrix non-linearity
- less on interlaminar shear stresses but may not be the case under fatigue load

Compressive strength of a multidirectional laminate

Stiffness Ratio Method :

$$\sigma_{\text{lam}} = \frac{\sigma_0^*}{N E_{11}} \sum_{k=1}^N n^{(k)} \cdot E_{x\theta}^{(k)}$$

σ_0^* critical stress for microbuckling initiation in the 0° ply



Theoretical predictions are conservative

Comparison of experimental and theoretical compressive strength for laminates $[(\theta/0_2)_2]_s$

Concluding remarks

The static compressive failure of UD and MD unnotched T800/924C carbon-fibre– epoxy laminates is controlled by fibre microbuckling.

Microbuckling initiates by the elastic bending of the 0° fibres, loaded by resin material in shear.

Its initiation depends on material imperfections, such as resin rich regions, voids and fibre misalignment (waviness).

Model shows the interlaminar shear stress has a small influence on the 0° fibre microbuckling initiation, while the fibre wavelength and matrix non-linearity have a more significant effect.

Average measured failure strains ε_{fav} for each of the four angles θ ($30^\circ, 45^\circ, 60^\circ, 75^\circ$) examined are scattered between -0.88 and -1%.

Specimens with $\pm 45^\circ$ surface plies appear to provide the most resistance to fibre microbuckling with $\varepsilon_{\text{fav}} = -0.95\%$.

The 0° -ply stress in a such laminate is ~ 1300 MPa compared to 1430 MPa measured for the 100% 0° laminate.

The 10% strength reduction could be due to edge effects and fabrication defects in the form of resin-rich regions and voids introduced at the interface of the axial and off-axis plies.